

Development and characterization of second order Band Pass Active Filter (BPAF)

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In electronic systems, the desired signal is much often than not overshadowed by unwanted signals. Attempt to amplify the wanted signals equally amplifies the unwanted one thereby increasing the ratio. Since signals are distinguished by their frequency characteristics, frequency selective circuits (Filters) can be used in filtering the wanted signals from the unwanted signal. Analog filter comes in different forms with different characteristics and can be active or passive. This paper presents the development and characterization of a second order band pass active filter. The active element used here is the Operational Amplifier OP AMP 741. The Transfer Function (TF) equation is derived and characterized with the Band Width (BW), Cut-off Frequencies (F_L and F_H), Center Frequency (F_C) and the Quality Factor (Q) specified and derived. The application of the developed Active Band Pass filter to signal of varied frequencies with fixed input voltage followed with the frequency response plots indicative of the designed specification.

Keywords — Active filter, band-pass, Operational Amplifier, Transfer Function, Band Width, Center frequency, Quality Factor.

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I. Introduction

The importance of filters in the world of electronics and telecommunication cannot be overemphasized. Filters cut off certain frequencies while enhancing desired frequencies. An electrical filter is a network designed to attenuate certain frequencies but pass others without attenuation [1]. Filters fall under two broad dimensions of Analog and Digital filters. Analog filter classified on their frequency response are Low-pass filter, High-pass filter, Band-pass filter, Band-stop filter and All-pass filter [2]. Analog filters can also be grouped under passive filter and active filters. The advantages of active filters over passive filter include but not limited to the following; absence of insertion loss, easy tuning, no isolation problem due to its high input impedance, pass band gain, flexibility in gain and frequency adjustment, small component size, absence of inductors and relative low cost[3]. Active filter thus gives more efficient, effective, portable and cheaper cost compared to passive filter.

The characteristics and terminologies of a band pass active filter are depicted in figure 1 below. A Band-Pass Filter(BPF) passes all the frequencies of signal between its two cut-off frequencies of lower frequency(f_L) and the higher frequency(f_H) with little or no attenuation and stops all other frequencies which are not within the range of frequencies. In BPF, The center frequency f_C is centered between f_L and f_H . and is related mathematically with F_L and f_H by the equation 1 below.

$$f_C = \sqrt{f_H f_L} \dots\dots\dots 1$$

The pass-band is the range of frequencies which are allowed to pass through to the output by the filter without any attenuation while the stop band is the range of frequencies which are not allowed to pass through to the output by the filter. Band pass filter has two stop bands, one before the pass band and the other after the pass band. A band-pass filter has a pass-band between two cut-off frequencies f_L and f_H There two types of band-pass filters viz:- wide band-pass filter and narrow band-pass filter. If the Quality factor(Q) is less than 10, it is narrow but if greater than 10, it becomes a wide band-pass filter[4] These are shown in figure 1 above.

It is pertinent to state that in practice, as opposed to the ideal case, the transition to stop bands are not sharp as indicated in the ideal band-pass characteristics as shown in figure 1. At the two cut-off frequencies f_L

and f_H the gain of the filter is down by 3dB[5]. This intermediate band formed between the pass-band and stop-band is known as transition band. The ideal band-pass filter and the practical band-pass filter are shown in figure 2 and 3 below respectively.

Band-pass filter could be achieved by connecting low-pass filter in series with high-pass filter though it is not the best approach practically [6].

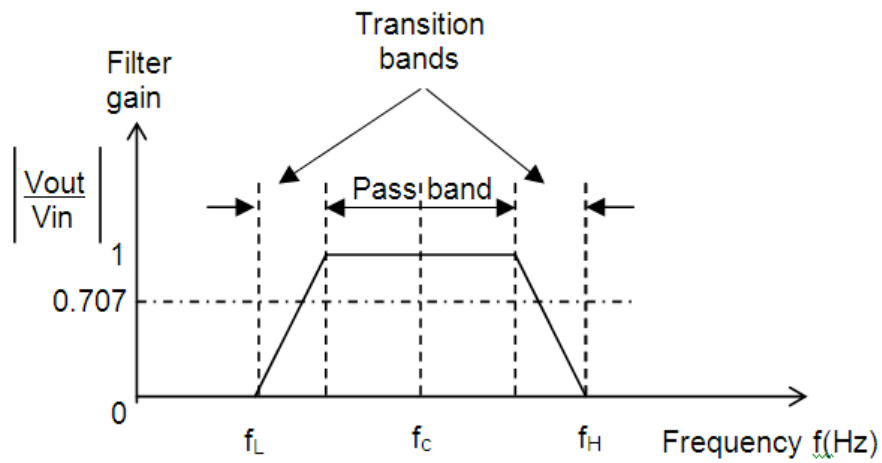


Fig 1: Practical band-pass filter

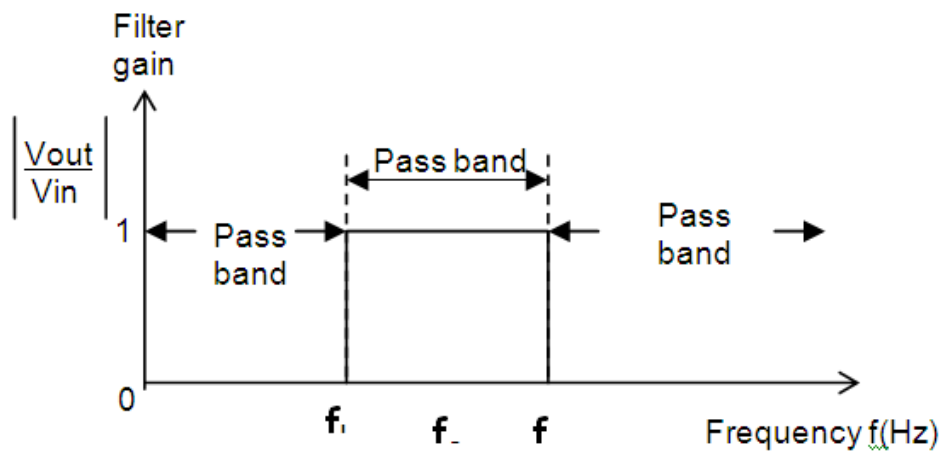


Fig 2: Ideal band-pass filter

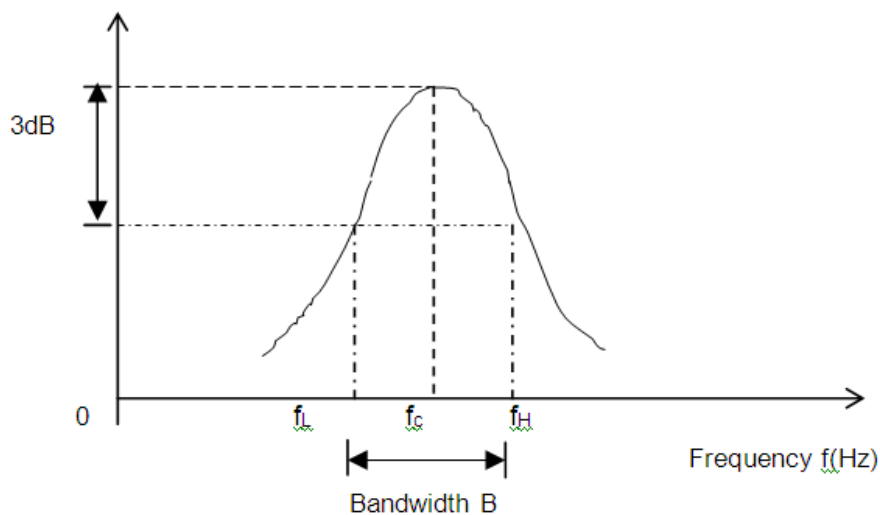


Fig 3: Practical band-pass filter frequency response

II. MATERIALS AND METHOD

2.1 LC Filter Simulation

An LC filter structure is the starting point in the design of active filters. This is done either by simulating each inductor by a gyro-capacitor combination or by transforming the basic filter structure such that it can be realized with General Impedance Convector (GICS) such as Frequency Dependent Negative Resistances (FDNRS)[7]. Both of the above methods of simulation can be realized with the Op-Amps. The circuit on inductance simulation using Op-Amp diagram in figure 4 below can be used for inductance simulation. In this circuit, the value of the inductance is given by the equation 1 below [8].

$$L = \frac{R_2 C (R_1 - R_2)}{1 + \omega^2 R_2^2 C^2} \text{ ----- 1}$$

By connecting a capacitor across x and y, a tuned circuit is obtained.

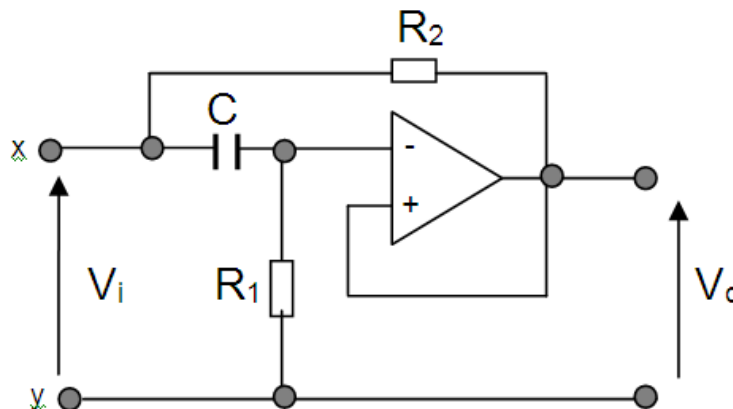


Figure 4: Inductance simulation by Op-Am

2.2 Transfer Function of second order filter

Transfer function (TF) is a mathematical equation which relates the output to the input signal as a function of the circuit components.[9] This plays an important role in filter design. Active filters are described by their order. This order is determined by the highest power of the polynomial which forms the denominator is the highest power of s, the laplace transform operator.

s ----- 1^{st} order

s^2 ----- 2^{nd} order

s^n ----- n^{th} order

Higher order of filters can be got by cascading of filters. The higher the order, the better is the frequency response characteristics of the filter so formed[10] The second order active band-pass filter under review is shown in figure 5 below.

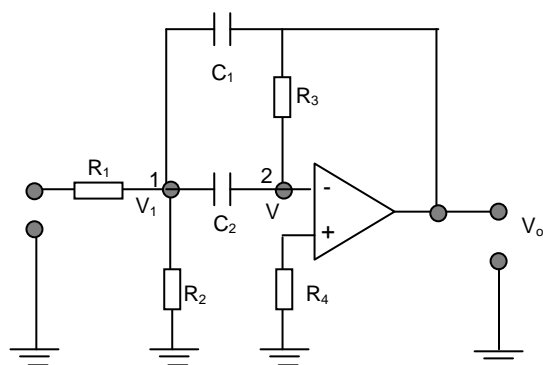


Figure 5: Second order multiple band-pass feedback filter

Analysis:

The op-amp is operating in its inverting mode while the nodal voltage approach is used in the analysis. Node 2 indicated below is at ground potential because the Op-Amp has very high open loop voltage gain A, and takes negligible current. This is the virtual earth concept and will be referred to from time to time throughout the analysis.

Taking Nodal voltage analysis at node 2:

Node 2 is at zero potential(virtual earth concept)

gives

$$sC_2V_1 - \frac{V_o}{R_3} = 0$$

$$V_1 = -\frac{V_o}{sC_2R_3} \quad - \quad - \quad 2$$

At node 1

$$\frac{V_1 - V}{R_1} + \frac{V_1}{R_2} + (V_1 - 0)sC_2 + (V_1 - V_o)sC_1 = 0 \quad - \quad - \quad 3$$

$$\frac{V_1}{R_1} - \frac{V}{R_1} + V_1sC_2 + sC_1V_1 - sC_1V_o = 0$$

$$V_1 \left(\frac{1}{R_1} + \frac{1}{R_2} + sC_2 + sC_1 \right) = \frac{V}{R_1} + V_o sC_1$$

$$V_1 \left(\frac{1}{R_1} + \frac{1}{R_2} + s(C_1 + C_2) \right) = \frac{V}{R_1} + V_o sC_1 \quad - \quad - \quad 4$$

Substituting the value of V_1 from equation 1 above

$$-\frac{V_o}{sC_2R_1R_2} \left(\frac{1}{R_1} + \frac{1}{R_2} + s(C_1 + C_2) \right) = \frac{V}{R_1} + V_o sC_1 \quad - \quad 5$$

$$-V_o \left(\frac{1}{sC_2R_1R_3} + \frac{1}{sC_2R_2R_3} + \frac{C_1 + C_2}{C_2R_3} + sC_1 \right) = \frac{V}{R_1} \quad - \quad 6$$

Multiplying both sides of equation 6 by sR_1 results in equation 7 below

$$-V_o \left(\frac{1}{C_2R_3} + \frac{R_1}{C_2R_2R_3} + \frac{s(C_1 + C_2)R_1}{C_2R_3} + s^2C_1R_1 \right) = sV \quad - \quad 7$$

$$\frac{V_o}{V} = \frac{s}{s^2C_1R_1 + s \left(\frac{R_1(C_1 + C_2)}{C_2R_2} \right) + \frac{1}{C_2R_3} \left(1 + \frac{R_1}{R_2} \right)} \quad - \quad 8$$

Equation 8 is the transfer function of the filter.

Dividing equation 8 through by C_1R_1 results in equation 9 below

$$\frac{V_o}{V} = \frac{\frac{s}{C_1 R_1}}{s^2 + \frac{1}{C_1 R_1} \left(\frac{R_1 (C_1 + C_2)}{C_2 R_3} \right) + \frac{1}{C_1 C_2 R_1 R_3} \left(1 + \frac{R_1}{R_2} \right)} \quad 9$$

$$\frac{V_o}{V} = \frac{\frac{1}{C_1 R_1} s}{s^2 + \frac{1}{R_3} \left(\frac{1}{C_1} + \frac{1}{C_2} \right) s + \frac{1}{C C R} \left(\frac{1}{R_1} + \frac{1}{R_2} \right)} \quad 10$$

2.3 CIRCUIT COMPONENT REALIZATION

The design features leading to component values and other filter characteristics are examined below using the derived transfer function. A standard transfer function of a second order filter is given in equation 11 below.

$$T.F. = \frac{-Ks}{s^2 + s(BW) + W_o^2} \quad \text{-----11}$$

Comparing equation 10 with the standard transfer function of equation 11, it could be deduced that

$$BW = s \left(\frac{1}{C_1} + \frac{1}{C_2} \right) \quad \text{-----12}$$

$$W_o = \sqrt{\frac{1}{C_1 C_2 R_3} \left(\frac{1}{R_1} + \frac{1}{R_2} \right)} \quad \text{-----13}$$

$$K = \frac{1}{C_1 R_1} \quad \text{-----14}$$

The capacitor values are fixed since it is easier to trim resistors to desired values.

Fixing $C_1 = C_2 = 1F$ -----14

And letting

$$\frac{R_1}{R_2} = n$$

$$R_1 = nR_2 \quad \text{-----15}$$

$$K = \frac{1}{C_1 R_2} = \frac{1}{R_1} \quad (C_1 = 1)$$

$$K = \frac{1}{nR_2} \quad \text{-----16}$$

$$BW = \frac{1}{R_3} \left(\frac{1}{C_1} + \frac{1}{C_2} \right) = \frac{2}{R_3}$$

$$R_3 = \frac{2}{BW} \quad \text{-----17}$$

Recall equation 13

$$\begin{aligned} W_o^2 &= \frac{1}{C_1 C_2 R_3} \left(\frac{1}{R_1} + \frac{1}{R_2} \right) \\ &= \frac{1}{R_3} \left(\frac{1}{R_1} + \frac{1}{R_2} \right) \\ &= \frac{1}{R_3} \left(\frac{1}{nR_2} + \frac{1}{R_2} \right) \\ &= \frac{1}{R_2 R_3} \left(\frac{1}{n} + 1 \right) \\ &= \frac{BW}{2} nk \left(1 + \frac{1}{n} \right) \end{aligned}$$

$$2W_o^2 = BWnk + BWK$$

$$n = \frac{2W_o^2 - KBW}{BWK} \text{-----18}$$

Thus the transfer function can be written as

Where BW = Bandwidth (in radians)

W_o = Centre Frequency (rad/s)

K = Gain constant

The following parameters are used for the filter under development

$$t, f = \frac{V_o}{V} = \frac{\frac{s}{nR_2}}{s^2 + \frac{2}{R_3}s + \frac{BW}{2} nK \left(1 + \frac{1}{N} \right)} \text{-----19}$$

From this equations derived and demonstrated so far, the component values of any filter with given parameters of Bandwidth(BW), Center frequency(f_o), and gain at center frequency can be computed.

The following parameters were used for testing the channels and the component values are as follows

Bandwidth (BW) = 6kHz

Center frequency (F_o) = 12.7kHz

Gain at center frequency (β_o) = -4db.

$$C_1 = C_2 = 20nF$$

$$R_3 = 2.7k\Omega$$

$$20 \log \left(\frac{\frac{1}{C_1 R_1}}{\frac{1}{BW}} \right) = 5dB$$

$$R_1 = 745.83\Omega \approx 750\Omega$$

From

$$R_2 = \frac{1}{\left(W_o^2 C_1 C_2 R_3 - \frac{1}{R_1} \right)}$$

$$R_2 = 180\Omega$$

Quality factor is sometimes referred to as the magnification factor. The higher the Q-factor, the more abrupt the transition phases of the frequency response curve and the narrower the bandwidth. The Q-factor gives information on the nature of the filter frequency response curve. This is of much importance in oscillators.

$$Q = \frac{f_o}{f_H - f_L} = \frac{f_o}{BW} \text{ --- } 20$$

$$= \frac{12.7}{6} = 2.11$$

2.4 ORGANIZATION AND TESTING

The filter circuit component assembled and in place was subjected to tests to ascertain the performance. With signal generator, a fixed input voltage (V_i) of 1Vp-p with varied frequency from 0.4kHz to 20.0kHz was injected to the filter input while the corresponding output voltages were measured. $20 \log \frac{V_o}{V_i}$ was computed

and tabulated with the other variables; Freq(Hz), V_i , V_o , $\frac{V_o}{V_i}$, $20 \log \frac{V_o}{V_i}$ (dB). The frequency response (dB vs

Freq) is shown on the graph in figure 6 below.

III. RESULTS AND DISCUSSION

The frequency of response plots of the developed second order band-pass filter are shown in figures 6 and 7 below. Figure 6 shows the response of the filter when 1volt peep-peek signal of varied frequencies (0.4kHz-20kHz) in order of 200Hz increment was used in the testing. The output voltage measured and tabulated. The gain, ratio of output voltage to the input (V_{out}/V_{input}) plotted against the corresponding frequencies plotted is shown in figure 6.

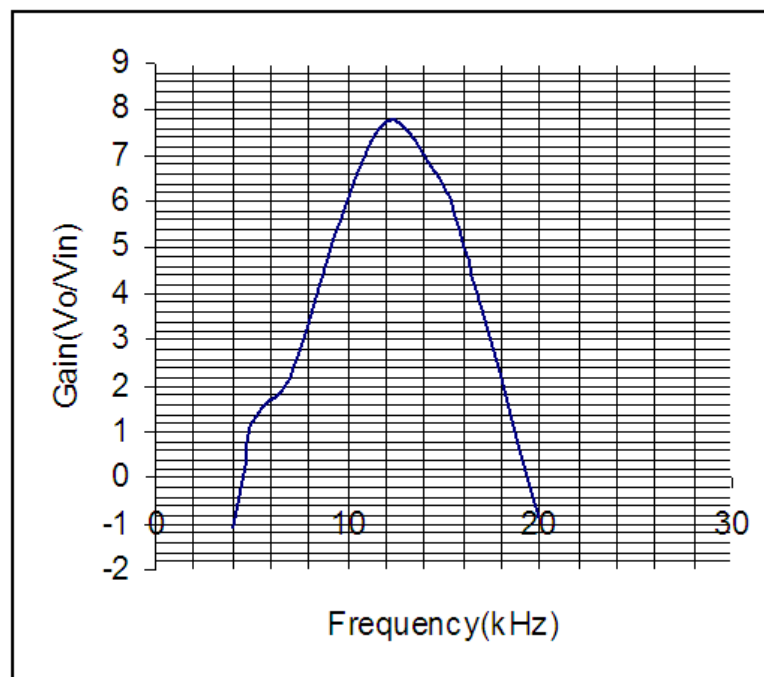


Figure 6: Frequency response of the 2nd order band-pass filter

Subsequently, a $20\log(V_{out}/V_{input})$ in decibel was plotted against their corresponding frequencies and plotted as shown in figure 7 below.

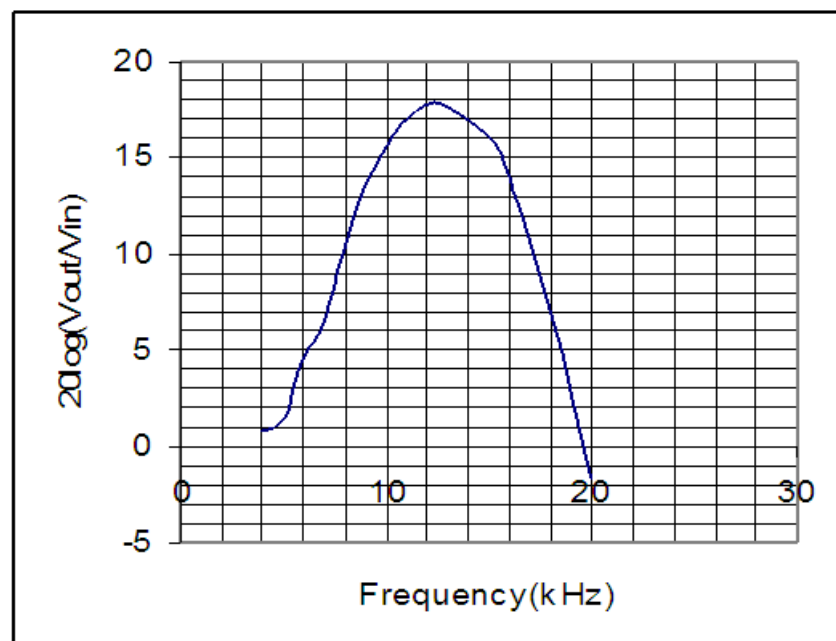


Figure 7: Freq response of filter with Gain in dB

IV. CONCLUSION

The proposed second order band-pass filter has successfully been developed and tested. The frequency response gives a good semblance of second order band-pass filter. This has shown the possibility of simulating inductances or coils out of circuit using active element in operational amplifier when used in its inverting mode. The accuracy becomes a function of choice in the wide range of parameters and the tolerances of the other passive components augmented alongside the active element of the operational amplifier.

REFERENCES

- [1]. Sanjay, S. Op-Amps and Linear Integrated Circuits, S.K. Kotari & Sons publishers(2010), New Delhi. pp.251-255
- [2]. Hughes, E. Electrical and Electronic Technology 10th edition, Pearson Education Ltd, Edinburgh, England, pp359.
- [3]. Maxfield Clive et al. Electrical Engineering: Know it all. Newness{2008}, Elsevier, Burlington, USA pp 621-625.
- [4]. Sanjay, S. Op-Amps and Linear Integrated Circuits, S.K. Kotari & Sons publishers(2010), New Delhi. pp.292-293.
- [5]. George C. and Steve W. Operational Amplifiers 4th edition, Butterworth-Heinemann (2000), Oxford, pp 20-23.
- [6]. Ezema E.E Design and construction of four channel graphic equalizer(unpublished) 1990 pp 45-48
- [7]. Harowitz P. and Hill W. The art of Electronics 2nd edition, Cambridge University Press(1989) pp266-267.
- [8]. Ezema E.E Design and construction of four channel graphic equalizer(unpublished) 1990 pp 45-48.
- [9]. Denton J. D. Operational Amplifiers and Linear integrated circuits, theory and applications, McGraw Hills, Inc 1989, USA pp66.
- [10]. Gottlieb I.M. Simplified Practical filter design. Tab Books 1st Edition, 1990 pp 1-4

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