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Evaluation of pipeline flanges subject to internal pressure and imposed external loads

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ABSTRACT: Engineers involved in pipeline design are often confronted with the evaluation of external loads imposed on flange connections. This article aims to provide more clarity in the various evaluation methods and the associated conservatisms. The magnitude of the external loads has an essential influence on the leak-tightness of the flange connection. Flange joint sealing integrity is of great importance and requires special attention. The article highlights various methods that can be applied in practice depending on the criticality of the pipeline system. Because various methods as described in this article are available to the engineer concerned, the sensitivity and degree of conservatism of the applied methods can be compared and evaluated. The successively discussed external flange load evaluation methods are: Comprehensive flange assessment approach based on ASME VIII-1; Appendix 2, Simple "Kellogg" based equivalent pressure approach, Improved "Kellogg" approach including "Koves" factor and evaluation method in accordance with ASME Code case 2901.

KEYWORDS: External loads, sealing integrity, degree of conservatism, external load evaluation methods.

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I. INTRODUCTION

The traditional flange calculation as included in ASME BPVC Section VIII - Division 1; Appendix 2 [1] does not account for imposed external loads that act together with the internal pressure on the flange connection. One of the most used conservative evaluation to perform flange check on external loads is the well known "Kellogg Equivalent Pressure Method", where the axial force F_E and the bending moment M_E are converted into an equivalent pressure P_{EO} . The equivalent pressure is then consecutively added to the internal design pressure and then compared with the rated pressure according to ASME B16.5 [2] or ASME B16.47 [3]. W.J. Koves has made a fundamental contribution to improving the conventional way of determining the equivalent pressure [4] and has been further elaborated by C.J. Dekker et al. [5]. Recently ASME Code case 2901 [6] has been published which offers an alternative for the assessment of welding neck flanges loaded by internal pressure and external loading. In some cases, however, it is desirable to perform a flange calculation that provides insight into the flange - and bolt stresses which occur in case of internal pressure in combination with external loads exerted on the flange. To accommodate this, the ASME flange calculation algorithm needs to be adjusted.

II. METHODOLOGY AND PRACTICAL APPROACH

The methodology recognizes the non-uniform load distribution due to bending moments and takes the flange rigidity into account to some extent. The flexibility of the flange, gasket and bolts should be modeled to sufficient accurately predict the gasket and bolt loads resulting from pressure and external loads. The flange can be analyzed by using the shell-and plate theory solution, which is consistent with the current ASME Code approach. The effect of axial loads on a flange joint can be handled the same way as the axial pressure thrust term in the current ASME method.

The axial force is simply added to the axial pressure - thrust force, and the ASME design procedure is followed for the computation of flange moments. Using ASME nomenclature:

$$H_D = \frac{\pi}{4}B^2.P + F_A$$

where:

 F_A = the axial applied force (only be taken into account if tensile) (N) P = the internal design pressure (MPa) B = the inside diameter of flange (mm) H_D = the axial force in the flange neck (N)

External moments are more difficult to handle. The loading is not axisymmetric and cannot be addresses as easily as the axial forces. However, the ASME design approach assumes axisymmetric behaviour. Therefore, the problem is to evaluate the effect of external moment loading on the flange joint and develop a correction to be applied to the axisymmetric analysis. This is addressed by analytically solving for the forces acting on a ring flange, as a result of an external moment; then comparing it with the axisymmetric force solution.

An external applied moment is assumed to create a linear stress distribution in the flange neck. This moment can be reduced to a linear distributed load. Therefore, a moment correction factor, F_M , can be defined which adjusts for the torsional resistance of the flange to external moment loads. Using the relationship between the shear modulus (G) and the Young's modulus of elasticity (E) being: $=\frac{E}{2(1+\nu)}$, which gives the following :

 $F_M = \frac{1}{\left[1 + \frac{J}{2(1+\gamma)I}\right]}$, where J and I are parameters related to flange configuration and rigidity.

where:

J = Polar moment of inertia (mm⁴),I = Second moment of inertia (mm⁴)

v = Poisson's ratio = 0.3.

 F_M is the reciprocal of the "Koves" factor K_f , hence,

$$F_M = \frac{1}{K_f}$$
 with $K_f = 1 + \frac{G.J}{E.I} = 1 + \frac{I_z + I_r}{2(1+v)I_r}$

where:

$$I_r = \frac{1}{12} \text{ (effective flange width) (flange thickness)}^3$$

$$I_z = \frac{1}{12} \text{ (flange thickness) (effective flange width)}^3$$
With v = 0.3 one arrives at: $K_f = 1 + \frac{(\text{effective flange width }, W_f)^2 + (\text{flange thickness }, t_f)^2}{2.6 \text{ (flange thickness }, t_f)^2}$

The effective flange width W_f is defined as the actual flange width being: 0.5 (OD flange - ID flange) minus the reduced bolt hole diameter D_{bhd} *.

The reduced bolt hole diameter follows from:

 D_{bhd} = max [Bolt hole diameter " D_{bhd} " (Inside diameter of flange "B" /1000 ; 0.5 x bolt hole diameter " D_{bhd} ")] Therefore:

$$K_f = 1 + \left[\frac{(t_f^2 + W_f - D_{bhd} *)}{(2.6 t_f^2)}\right] \text{ and } F_M = \frac{1}{K_f}$$

The greater the torsional resistance, relative to the bending resistance, the less the induced circumferential bending stress and corresponding flange rotation as a result of the external moment.

Using the terminology of ASME Section VIII, Division 1 - Appendix 2 [1], external moments and forces can be included in the design by defining the operating design moment as follows:

$$H_D = \frac{\pi}{4}B^2.P + F_A + \frac{4F_{M.}M_E}{G}$$
(N)

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 $H_{G} = (2b)(\pi. G. m. P) \quad (N)$ $H_{T} = \frac{\pi}{4}(G^{2} - B^{2})P \quad (N)$ $M_{O} = H_{D}.h_{D} + H_{T}.h_{T} + H_{G}.h_{G} \quad (Nmm)$

The rest of the flange calculation is performed in accordance with the procedure described in ASME VIII-1, Appendix 2[1].

A fully elaborated example is given in Section III of this article.

III. WORKED EXAMPLE

A welding neck flange connection in accordance with ASME B16.47 Series A Class 300 is part of an NPS 36 " (NB 900) gas transmission pipeline.

The design conditions are:

Design pressure 30 bar, design temperature 50° C, corrosion allowance nil.

The flange connection is provided with a spiral wound gasket according to ASME B16.20 [7]. The flange material is A105, bolt material is A193 B7 and the pipeline material is A515 Grade 70.

The external loads acting on the flange connection are respectively: $F_A = F_E = 350$ kN and the resulting bending moment $M_E = 330$ kNm.

Moment M_E is initially based on a bending stress in the adjoining pipe of 6000 psi = 41.37 MPa whilst the axial tensile force F_A is based on approximate 0.2 times the hydrostatic end force. This rule of thumb is often used by practicing engineers as a starting point.

Calculation

The execution of the calculation is limited to the operating condition and is shown in table 1 below.

| Table 1. | | | | |
|--|--------------------------------|------------------|----------------------|-----------------------|
| Flange Calculation (Type Integral Flange) | | | | |
| Welding Neck Flange according ASME B16.47 ; NPS 36" ; Series A ; Class 300 | | | | |
| System Design | Parameter | Symbol | Value | Equation |
| Parameters | Design Pressure | Р | 3 MPa | |
| | Design Temperature | - | 50°C | |
| | Axial Force | $F_A = F_E$ | 350 kN | |
| | Bending Moment | M _E | 330 kNm | |
| Flange Data | Flange outside diameter | А | 1270 mm | |
| | Flange inside diameter | В | 889 mm | |
| | Bolt circle diameter | С | 1168.4 mm | |
| | Flange thickness | t _f | 103.2 mm | |
| | Hub thickness small end | g _o | 12.7 mm | |
| | Hub thickness large end | g1 | 51 mm | |
| | Hub length | h | 136.8 mm | |
| | Bolt hole diameter | D _{bhd} | 54 mm | |
| Bolting data | Bolt size | D _b | 2" UN | |
| | Number of bolts | n _b | 32 | |
| Gasket data | Gasket material | - | SPW | |
| | Gasket factor | m | 3 | |
| | Gasket seating stress | у | 69 MPa | |
| | Outside diameter gasket | God | 1003.6 mm | |
| | (Effective) | | (include bead of 1.5 | |
| | | | mm) | |
| | Inside diameter gasket | G _{ID} | 955.8 mm | |
| | Gasket width | N | 23.9 mm | $(G_{OD} - G_{ID})/2$ |
| | Basic gasket seating width | bo | 11.95 mm | N/2 |
| | Effective gasket seating width | b | 8.71 mm | 2.52 √b₀ |
| | Gasket load reaction diameter | G | 986.18 mm | G _{OD} - 2.b |

| Calculation | Radial distance | R | 88.7 mm | $R = (C-B)/2 - g_1$ |
|-------------|--|-------------------|---------------|---|
| parameters | Lever arm | h _D | 114.2 mm | $R + 0.5 g_1$ |
| | Lever arm | h _T | 115.41 mm | $(R + g_1 + h_G)/2$ |
| | Flange width | W _f | 190.5 mm | (A - B)/2 |
| | Reduced bolt hole diameter | D _{bhd*} | 48 mm | $D_{bhd*} = max [D_{bhd} (B/1000; 0.5)]$ |
| | | | | D _{bhd}) |
| | Moment correction factor | F _M | 0.7195 | $F_M = \frac{1}{K_f}; K_f = 1 +$ |
| | | | | $\left[\frac{\left(t_{\rm f}^2+W_{\rm f}-Dbhd*\right)}{\left(2.6t_{\rm f}^2\right)}\right]$ |
| | Lever arm | h _G | 91.11 mm | (C-G)/2 |
| | Hydrostatic end force inside | H _D | 3175200 N | $H_D = \frac{\pi}{4}B^2.P + F_A + \frac{4.F_M.M_E}{G}$ |
| | Difference H - H _D is pressure force at flange face | H _T | 429369 N | $H_T = \frac{\pi}{4} (G^2 - B^2) P$ |
| | Gasket load for sealing | H _G | 485732 N | $H_G = (2b)(\pi.G.m.P)$ |
| | Flange moment | Mo | 456416359 Nmm | $M_0 = H_D, h_D + H_T, h_T + H_C, h_C$ |

Flange factors

Bolt spacing factor $B_{SC} = 1.0$ (as per code)

 $\begin{array}{l} \mathsf{K} = \mathsf{A}/\mathsf{B} = 1.4286 \ ; \ \mathsf{h}_{O} = \sqrt{B} \ g_{O} = 106.2558 \ ; \ \mathsf{h} \ / \ \mathsf{h}_{O} = 1.2875 \ ; \ \mathsf{T} = 1.7418 \ ; \ \mathsf{Z} = 2.9216 \ ; \ \mathsf{Y} = 5.6113 \ ; \\ \mathsf{U} = 6.1662 \ ; \ \mathsf{F} = 0.6124 \ ; \ \mathsf{V} = 0.0415 \ ; \ \mathsf{f} = 1.0 \ ; \ \mathsf{e} = 0.00576 \ (1/\text{mm}) \ ; \ \mathsf{g}_1 \ / \ \mathsf{g}_{O} = 4.0157 \ ; \\ \mathsf{d} = 2545760.9284 \ (\text{mm}^3) \ ; \ \mathsf{L} = 1.3474 \ ; \ \mathsf{E} = 200666 \ \text{MPa} \ ; \ \mathsf{K}_{\mathrm{I}} = 0.3 \end{array}$

| Stresses under operating condition | | | | |
|--|------------|---------------------|--|--|
| Equation | Value | Allowable stress | | |
| $f M_0$ | 146.49 MPa | 1.5 x 138 = 207 MPa | | |
| $S_H = \frac{1}{L g_1^2 B}$ | | | | |
| $(1.33 t_f e + 1) M_0$ | 64.06 MPa | 138 MPa | | |
| $S_R = \frac{1}{L t_f^2 B}$ | | | | |
| Y M ₀ | 83.34 MPa | 138 MPa | | |
| $S_T = \frac{1}{t_f^2 B} - Z S_R$ | | | | |
| $S_{\rm C} = {\rm Max} \left[(S_H + S_R)/2 ; (S_H + S_T)/2 \right]$ | 114.91 MPa | 138 MPa | | |
| Flange rigidity check | | | | |
| 52.14 V M_{0} | 0.7104 | ≤ 1.0 | | |
| $J = \frac{1}{L E g_0^2 K_1 h_0}$ | | | | |
| Verification of bolt stress during operating | | | | |
| Bolt force required for operating: $W_{m1(tot)} = H + H_P + F_A + \frac{4M_E}{C} = \frac{\pi}{A}G^2P + (2b)(\pi.G.m.P) + F_A + \frac{4M_E}{C}$ | | | | |
| $W_{m1(tot)} = 2777251 + 350000 + 4 \times 330000000 / 1168.4 = 4257001 N$ | | | | |
| Bolt stress $S_{bolt} = W_{m1(tot)} / (n_b x A_{bolt}) = 4257001 / 32 x 1710.9 = 77.76 MPa < 172 MPa (A193 B7 bolting)$ | | | | |

IV. DISCUSSION

For comparison with the case detailed in Section III, an evaluation will be performed using:

- A. Kellogg's equivalent pressure method
- B. Kellogg's method including "Koves" factor

C. ASME Code Case 2901

The results of the tabulated comparison are shown below in Table 2.

Table 2.

| Method "A" | Method "B" | Method "C" | | |
|---|---|--|--|--|
| By the "Kellogg" Equivalent Pressure | As method "A" however the moment | Method developed by Warren Brown and released in | | |
| Method, a Peq is determined, added to | term is divided by the "Koves" factor | ASME code as case 2901. | | |
| the design pressure P and then | "K _f " | | | |
| compared to the flange | | | | |
| rated pressure at the operating / | | | | |
| design temperature. | | | | |
| Condition to be satisfied | Condition to be satisfied | Condition to be satisfied | | |
| $P + P_{eq} \le P_{rating} = 5.01 \text{ MPa}$ | $P + P_{eq} \le P_{rating} = 5.01 \text{ MPa}$ | $16 M_{E} + 4 F_{E} G \le \pi G^{3} [(P_{R} - P_{D}) + F_{M} P_{R}]$ | | |
| | | 6660652000 < 7565979451 | | |
| $P + \frac{4 F_A}{2} + \frac{16 M_E}{2} = 5.21 \text{ MPa}$ | $K_{\rm f} = 1 / F_{\rm M} = 1.39$ | | | |
| $\pi G^2 = \pi G^3$ | | OK! | | |
| $> 5.01 MP_{3}$ | $P + \frac{4 F_A}{r^2} + \frac{16 M_E}{r^2 W} = 4.72 \text{ MPa}$ | | | |
| > 5.011011 a | $\pi G^2 = \pi G^3 K_f$ | Where: | | |
| | < 5.01 WH a | $M_E = External moment$ | | |
| NOT OK | OKI | F_E = External tensile axial force | | |
| | OK: | G = Gasket reaction diameter | | |
| | | | | |
| | | | | |

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| Pseudo flange design pressure: Case #1 = 5.21 MPa | Pseudo flange design pressure: Case #2 = 4.72 MPa | | P_R = Flange pressure rating at design temperature P_D = Flange design pressure at design temperature F_M = Moment factor = 0.1 according to table 1 of case 2901. | | |
|--|--|---|---|---------------|---------------------|
| Corr | #1 with d | Stresses under oper | ating cond | ition | 5702 Nmm |
| Case | 2 #1 with d | esign pressure = 5.21 esign pressure= 4.72 l | MPa and M | $c_0 = 33222$ | 9926 Nmm |
| Equation | | Value Case #1 | Value Cas | se #2 | Allowable stress |
| $S_H = \frac{f M_0}{L g_1^2 B}$ | | 170.83 MPa | 154.77 M | Pa | 1.5 x 138 = 207 MPa |
| $S_R = \frac{(1.33 t_f e + 1)M_0}{L t_e^2 B}$ | | 74.73 MPa | 67.70 MP | a | 138 MPa |
| $S_T = \frac{Y M_0}{t_f^2 B} - Z S_R$ | | 97.11 MPa | 87.98 MP | a | 138 MPa |
| $S_{\rm C} = {\rm Max} \left[(S_H + S_R)/2 ; (S_H + S_T)/2 \right]$ | | 133.97 MPa | 121.37 M | Ра | 138 MPa |
| Flange rigidity check | | | | | |
| $J = \frac{52.14 \text{ V M}_{0}}{\text{L E g}_{0}^{2} \text{ K}_{1} \text{h}_{0}}$ | | 0.83 | 0.75 | | ≤ 1.0 |
| It appears that the stresses for cases #1 and #2 are higher than for the case elaborated in table 1, indicating that Methods "A" and "B" are | | | | | |

more conservative than those applied in table 1.

In line with the previous calculations and assessments, we increase the magnitude of the external loads such that an optimum flange stress is achieved, resulting in F_A (F_E) is 562 kN and M_E is 530 kNm.

The result of this exercise is shown in table 3 below.

| Table 3. | | | | |
|---|------------|---------------------|--|--|
| Stresses under operating condition with $F_A = F_E = 562$ kN and $M_E = 530$ kNm | | | | |
| Equation | Value | Allowable stress | | |
| $S_H = \frac{f M_0}{L g_1^2 B}$ | 175.66 MPa | 1.5 x 138 = 207 MPa | | |
| $S_R = \frac{(1.33 t_f e + 1)M_0}{L t_f^2 B}$ | 76.82 MPa | 138 MPa | | |
| $S_T = \frac{Y M_0}{t_f^2 B} - Z S_R$ | 99.92 MPa | 138 MPa | | |
| $S_{\rm C} = {\rm Max} \left[(S_H + S_R)/2 ; (S_H + S_T)/2 \right]$ | 137.79 MPa | 138 MPa | | |
| Flange rigidity check | | | | |
| 52.14 VM_0 | 0.852 | ≤ 1.0 | | |
| $J = \frac{1}{L E g_0^2 K_1 h_0}$ | | | | |
| Verification of bolt stress during operating | | | | |
| Bolt force required for operating: $W_{m1(tot)} = H + H_P + F_A + \frac{4M_E}{C} = \frac{\pi}{4}G^2P + (2b)(\pi.G.m.P) + F_A + \frac{4M_E}{C}$ | | | | |
| $W_{m1(tot)} = 2777251 + 562000 + 4 \times 530000000 / 1168.4 = 5153698 N$ | | | | |
| Bolt stress S _{bolt} = W _{m1(tot}) / (n _b x A _{bolt}) = 5153698 / 32 x 1710.9 = 94.13 MPa < 172 MPa (A193 B7 bolting) | | | | |

Table 4 provides insight into the permissible set of loads (F_E or F_A and M_E) for which the condition is just fulfilled.

| I able 4. | | | | |
|---|---|--|--|--|
| Method "A" | Method "B" | Method "C" | | |
| By the "Kellogg" Equivalent Pressure | As method "A" however the | Method developed by Warren Brown [8] and | | |
| Method, a Peq is determined, added to the | moment term is divided by the | released in ASME code as case 2901. | | |
| design pressure P and then compared to the | "Koves" factor "K _f " | | | |
| flange rated pressure at the operating / | | | | |
| design temperature. | | | | |
| Condition to be satisfied | Condition to be satisfied | Condition to be satisfied | | |
| $P + P_{eq} \le P_{rating} = 5.01 \text{ MPa}$ | $P + P_{eq} \le P_{rating} = 5.01 \text{ MPa}$ | $16 M_{\rm E} + 4 F_{\rm E} G \le \pi G^3 [(P_{\rm R} - P_{\rm D}) + F_{\rm M} P_{\rm R}]$ | | |
| | | | | |
| With: | $K_{\rm f} = 1 \ / \ F_{\rm M} = 1.39$ | Where: | | |
| $F_A = 318 \text{ kN}$ and | | $M_E = External moment$ | | |
| $M_E = 300 \text{ kNm}$ | With: | F_E = External tensile axial force | | |
| we end up to: | $F_A = 408 \text{ kN}$ and | G = Gasket reaction diameter | | |
| | $M_E = 385 \text{ kNm}$ | P_R = Flange pressure rating at design temperature | | |
| $P + \frac{4 F_A}{c^2} + \frac{16 M_E}{c^3} = 5.01 \text{ MPa}$ | we end up to: | P_D = Flange design pressure at design temperature | | |
| $\pi G^2 = \pi G^3$ | | F_M = Moment factor = 0.1 | | |
| | $P + \frac{4 F_A}{c^2} + \frac{16 M_E}{c^3 K} = 5.01 \text{ MPa}$ | | | |
| Index with respect to F_{E} is 562 kN and M_{E} | $\pi G^2 = \pi G^3 K_f$ | With: | | |
| | | | | |

Table 4.

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|---|---|---|--|--|
| is 530 kNm according to optimum ASME flange calculation:0.566 | Index with respect to F_E is 562 kN and M_E is 530 kNm according to optimum ASME flange calculation: 0.726 | $F_E = 397 \text{ kN and}$ $M_E = 375 \text{ kNm}$ we end up to: | | |
| | | $\begin{array}{l} 7566053840 ~7565979451 \\ \hline \textbf{Index} \text{ with respect to } F_{E} \text{ is } 562 \text{ kN} \text{ and } M_{E} \text{ is } 530 \\ \text{kNm according to optimum ASME flange} \\ \text{calculation: } \textbf{0.707} \end{array}$ | | |

The index of conservatism (also called the compatibility index) is a way of indicating the difference in effect between two or more methodologies. The lower the index, the higher the degree of conservatism.

The figure below shows in graphic form the conservatism indexes associated with the various approaches.



In addition the maximum allowable internal pressure has been calculated for the flange under consideration without taking into account external loads exerted on the flange. Only the operating condition has been considered and the pressure has been optimized to the allowable flange stresses and the rigidity requirement. The result led to an allowable pressure of 53.65 bar (5.365 MPa). The rated pressure according to ASME B16.47 is 50.1 bar (5.01 MPa) for this flange, which equates to a difference of about 7%.

It could be argued that the difference between the rated flange pressure or the calculated allowable pressure of the flange and the design pressure is left over for the external loads imposed on the flange connection. Often in practice the external load is converted to an equivalent pressure and added to the design pressure. This allows a resultant calculation pressure that can be used in the traditional flange calculation according to ASME. The bending moment is the dominant loading in this approach and is very popular among piping engineers and there is little doubt about the usefulness of this approach.

V. CONCLUSION

For the flange connection in question, it can be concluded that the adjusted analytical flange calculation according to ASME provides a reliable insight into the flange stresses that occur when the flange connection is loaded by internal pressure and external loads exerted on it. The flange and bolt stress is amply permissible for the initial condition considered. Adjusted in this context means that the common ASME method is augmented with terms related to the imposed external loads. In the case that this flange configuration is evaluated using the simple "Kellogg" equivalent pressure method "A", the assessment condition is found not to be met. If, on the other hand, the so-called "Koves" factor is introduced in the case of method "B", it appears that the external flange loads are permissible. This also applies when applying ASME Code case 2901 for this flange connection. Note that both Method "B" and Method "C" are fairly easy to apply and can give a quick impression of the criticality of the external loads. If we observe table 4, we discover that all three methods are more conservative than the adjusted ASME flange calculation method which include the external loads. It is also striking that for

the considered flange method "A" is most conservatively followed by method "C" and "B". The mutual differences between Method "B" and "C" are relatively small.

VI. CONCLUDING REMARKS

In order to be able to state that the research conducted is sufficiently representative, it is recommended to extend the analyzes to more flange dimensions and pressure classes.

Although this investigation has been limited to one flange diameter and pressure class, the result provides sufficient starting points for further investigation and also an indication of the preferred method for evaluating external flange loads.

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