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**Research** Paper

## **ELECTROHYDRAULIC SYSTEM FOR AUTOMATIC GAGE CONTROL** (AGC) FOR TANDEM COLD MILL PLANT IN SARTID SMEDEREVO

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Abstract: Electro hydraulic servosystem for the AGC has better characteristics than electromechanic (five timesgreater speed of rolling, greater speed of positioning ,smaller dead-zone, smaller time of roll gap adjusting start, smaller time of maximum speed reaching, greater unloading speed).

Keywords: Automatic control system, electromenechanical, electrohydraulic system, mechanical system, servovalve.

#### I. **INTRODUCTION**

In Hot and Cold Mill Plants were mounted electrohydraulic servosystems for automatic gage control (instead electromechanic systems with screw thread) during modernisation. For the applications of the mostly control algorithms are necessary knowledge of mathematical models as components as complete object of automatic control. Detail analysis of these servosystems will help for better understanding and for the next optimisations by applications of modern control methods. This work is based on results from literature [1].

#### II. ELECTROMECHANICAL SYSTEM FOR AUTOMATIC GAGE CONTROL

Automatic control system works on the following manner: if aberation of the strip thickness at the stand exit is happened then a signal from a thickness gage 9 by converter is led to summator 14 where this signal compares with set up signal. Error signal is led to regulator and from regulator to electromotor 13. .Electromotor 13 moves screw and changes rolling force and thickness of streep too. The greater disadvantage of this regulation type is the great friction between screw and screw nut which disable very quick and very precision work.



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### III. **ROLLING STANDS ELASTIC DEFORMATION AND PLASTIC DEFORMATION CURVE**

Sum of elastic deformations of the all loaded rolling stand parts is rolling stand elastic deformation. Elastic deformation of rolling stand can be determined by theoretical or experimental method(theoretical method is rarely used because it is hard to determine the clearances between parts of rolling stand).



Figure 3. Curve of elastic deformation of the rolling stand

From the figure 3 is possible to write equation (1):

$$\mathbf{H}_{i} = \mathbf{H}_{os} + \frac{F_{p}}{E_{c}} \tag{1}$$

the following symbols are defined:

 $\mathbf{H}_{1}$  - strip thickness at the exit from the rolling stand,

 $H_{a}$  - value of the initial gap between rolls,

 $\mathbf{F}_{\mathbf{r}}$  - modulus of rolling stand elasticity.

Therefore equation (1) contains two unknown values (rolling force and thickness of the strip at the exit from the stand) it is necessary to know dependence of rolling force from exit strip thickness for a concrete rolling conditions (entry strip thickness, friction coefficient, rolls diameters...). Desired dependence is given by equation(2):

 $F_{p} = f(H_{u}, R, \lambda....)$  (2)

Curves given by equation (2) are strip plastic deformation curves(curves of plasticity and it is possible to obtain its by theoretical or experimental method. Figure 4 shows plastic deformation curve of strip.



From figure 4 it is obvious that greater rolling force enables smaller strip thickness at the rolling stand exit. Simultaneously equations (1) and (2) solvings give rolling force and exit strip thickness during strip deformation in real working stand. Graphic equations solution is shown on figure 5.

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Figure 5. Graphic determination of the rolling force

Section n the straight line 1- the curve 2 determines point A. The coordinates of the point A ( $F_{p1}$  and  $H_1$ ) determine rolling force  $F_{p1}$  which must act on the rolls to perform exit strip thickness  $H_1$ . The gap between rolls increases from  $H_{os}$  to  $H_1$  until thickness of the strip reduced from  $H_{os}$  at entry of the stand to  $H_1$  at the exit of the stand. In the process computer are "memorized" straight line 1 and curve 2 and for demand  $H_1$  it is possible to determinate  $F_{p1}$  and  $H_{os}$  (it is necessary to draw a vertical line from the point  $H_1$  and point of section with the curve 2 is point A; From point A it is necessary to draw a horizontal line and obtain  $F_{p1}$ : It is necessary to draw a line through a point A with angle and obtain  $H_{os}$ . However, if the strip has the greater hardness then the rolling force Fp1 will not be sufficient to perform  $H_1$  and control system will increase the rolling force  $F_{p1}$  to get demand thickness of the strip at the exit of the stand.

### IV. SERVOVALVE

Therefore a reprensentation of servovalve response throught the frequency range about 50 cps is sufficient (literature [1]), and a first-order expression is adequate. The time constant for the first-order transfer function is best established by 0.7 amplitude point (-3 db) (figure 6). Figure 6 shows a "Moog" servovalve dynamic response,together with the response of a first-order transfer function. The first-order aproximation is a quite good throught the lower frequency region. According to literature [2] and figure 6 we can write:



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## American Journal of Engineering Research (AJER) 2013 v. SERVOVALVE CONTROLLED PISTON $P_{i}$ 0 $IQ_2$ $X_k$ $m_{i}$ $P_c$ $V_{l}$ $A_c$ $V_2$ $Y_c$ Figure7. Servovalve controlled cylinder piston Figure 7. Servovalve controlled cylinder piston $p_c$ ; $F_{pc} = p_c A_c$ ; force induced by roll stand elasticity:

force of inertia:  $F_{in} = m_c \frac{d^2 Y_c}{dt^2}$ while:  $m_c = m_T + m_{kc}$ ;  $m_T - load$  mass,  $m_{kc}$  - mass of the cylinder piston,  $m_c$  - "common" mass .

Force of friction in the gaskets is negligible because the gaskets are made from a special PTFE material. The Second Newton's law for cylinder piston is given by equation (5):

$$p_{c}A_{c} = m_{c}\frac{d^{2}Y}{dt^{2}} + E_{sT}Y.$$
(5)

Cylinder entry flow  $(Q_c)$  is consist of the flow for the piston moving  $Q_v$  and flow for the compressibility compensation  $Q_{LC}$ , while leakage is negiglible. We can write flow equation (6):

$$\mathbf{Q}_{c} = \mathbf{A}_{c} \frac{\mathrm{dY}}{\mathrm{dt}} + \frac{\mathbf{V}}{\mathrm{B}} \frac{\mathrm{dp}_{c}}{\mathrm{dt}}.$$
 (6)

Flow which leaves servovalve is:

$$Q_{sR} = \mu_{sR} W_{sR} X_{\kappa} \sqrt{\frac{2}{\rho} (p_s - p_c)}$$
(7)

We can combine equations (5) and (6) to yield equation (8):

$$\mu_{\text{SR}} W_{\text{SR}} X_{\text{K}} \sqrt{\frac{2}{\rho} (p_{\text{S}} - p_{\text{C}})} = A_{\text{c}} \frac{dY}{dt} + \frac{V}{B} \frac{dp_{\text{c}}}{dt} \cdot (8)$$

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 $\mathbf{F}_{\mathbf{x}} = \mathbf{E}_{\mathbf{ST}} \mathbf{Y}_{\mathbf{x}}(4)$ 

### VI. GAUGES, TRANSDUCERS AND SIGNAL AMPLIFIERS

From literature [1] we can write equations for the position gage, transducer and signal amplifier:

$$W_{MP} = \frac{U_{MP}(s)}{Y_{c}(s)} = \frac{K_{PC}}{T_{u}S'+1}, (9)$$
$$U_{y} = C_{1}H_{iy}, \qquad (10)$$

$$\mathbf{I} = \mathbf{K}_{A} (\mathbf{U}_{y} - \mathbf{U}_{MP})^{(11)}$$

while:  $W_{_{MP}}$  – transfer function for piston rod position gage together with the position-voltage transducer,  $U_{_{MP}}$  - exit signal from the position gage,  $H_{_{iy}}$  - demand piston rod position signal,  $C_{_1}$  - amlification of demand position signal,  $K_{_{A}}$  - amplification of voltage-current transducer.

### VII. MATHEMATICAL MODEL OF A ROLLING STAND Linearisation of equation (1) gives equation (12):

$$H_i = H_{osi} + \frac{F_p}{E_s}$$
 is given by:

$$\mathbf{H}_{i} = \mathbf{H}_{in} + (\mathbf{H}_{osi} - \mathbf{H}_{osin}) \frac{\partial \mathbf{H}_{i}}{\partial \mathbf{H}_{osi}} + (\mathbf{F}_{p_{i}} - \mathbf{F}_{p_{in}}) \frac{\partial \mathbf{H}_{i}}{\partial \mathbf{F}_{p_{i}}}$$
(12)

From equations (1) and (12) we can write equation (13) (in relative variations):

$$h_{i} = \frac{H_{OSIN}}{H_{IN}}h_{osi} + \frac{F_{pin}}{H_{in}E_{si}}f_{pi} = h_{i} = l_{1i}h_{osi} + l_{2i}f_{pi}.$$
(13)

We consider cylinder piston rod, bottom work roll and bottom back up roll as "common" unit and therefore piston rod position change is the same as roll gap change. Therefore we can write equation (14):

$$\mathbf{h}_{i} = \mathbf{l}_{1i} \mathbf{y}_{c} + \mathbf{l}_{2i} \mathbf{f}_{pi}$$
 (14)

In the literatures [1] and [3] we can find equation (14) for the any of Sartid Cold Mill stand:

$$F_{pi} = \lambda_{1}F_{K_{1i}} + (1 - \lambda_{1})F_{K_{2i}} - \frac{2}{3}F_{ZZi} - \frac{1}{3}F_{ZPi} \cdot \sqrt{R(Hu_{i} - H_{i})}, \quad 0, 6 + 0, 4\sqrt{\frac{H_{i}}{H_{ui}}}e^{\frac{\mu\sqrt{R_{i}(H_{ui} - H_{i})}}{(12H_{i} + 0.28H_{ui})}} + \frac{2}{3}a_{4}\sqrt{R_{i}H_{i}}\left(F_{K_{2i}} - F_{zpi}\right)^{\frac{3}{2}}$$
(15)

where:

 $F_{K_1} = a_1 (a_2 + \frac{H_{ui}}{H_0})^{a_3}$   $F_{K_2} = a_1 (a_2 + \frac{H_{ui}}{H_5})^{a_3}$ 

For the soft steel are:

$$a_1 = 55,3; a_2 = 1,002; a_3 = 0,27; \lambda_1 = 0,2; a_4 = \sqrt{\frac{1 - \gamma^2}{E}},$$

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 $\mathbf{F}_{xxi}$  - force of back tension,

 $F_{mi}$  – force of front tension,

R – work roll diameter,

 $\mathbf{H}_{0}$  - thickness of the strip at the first stand entry,

H<sub>5</sub>- thickness of the strip at the last stand exit.

Therefore we can write equation (16):

$$F_{pi} = (H_{ui}, H_i, F_{zzi}, F_{zpi}).$$
 (16)

We can obtain equation (16) (in relative variations) by linearisation of equation (15):

$$\mathbf{f}_{pi} = \frac{\mathbf{H}_{in}}{\mathbf{F}_{pin}} \frac{\mathcal{F}_{pi}}{\mathcal{H}_{i}} \left| \mathbf{h}_{i} + \frac{\mathbf{H}_{uin}}{\mathbf{F}_{pin}} \frac{\mathcal{F}_{pi}}{\mathcal{H}_{ui}} \right| \mathbf{h}_{ui} + \frac{\mathbf{F}_{zzin}}{\mathbf{F}_{pin}} \frac{\mathcal{F}_{pi}}{\mathcal{F}_{zzi}} \left| \mathbf{f}_{zzi} + \frac{\mathbf{F}_{zpin}}{\mathbf{F}_{pin}} \frac{\mathcal{F}_{pi}}{\mathcal{F}_{zpi}} \right| \mathbf{f}_{zpi} + \mathbf{q}_{1i} \mathbf{h}_{i} + \mathbf{q}_{2i} \mathbf{h}_{ui} + \mathbf{q}_{3i} \mathbf{f}_{zzi} + \mathbf{q}_{4i} \mathbf{f}_{zpi}.$$
(1)

We can combine equations (12) and (17) and write equation (18):

$$\mathbf{h}_{i} = \frac{\mathbf{l}_{ii}}{1 - \mathbf{l}_{2i}\mathbf{q}_{1i}} \mathbf{y}_{ci} + \frac{\mathbf{l}_{2i}\mathbf{q}_{2i}}{1 - \mathbf{l}_{2i}\mathbf{q}_{1i}} \mathbf{h}_{ui} + \frac{\mathbf{l}_{2i}\mathbf{q}_{3i}}{1 - \mathbf{l}_{2i}\mathbf{g}_{1i}} \mathbf{f}_{zzi} + \frac{\mathbf{l}_{2i}\mathbf{q}_{4i}}{1 - \mathbf{l}_{2i}\mathbf{q}_{1i}} \mathbf{f}_{zpi} + \mathbf{a}_{1i}\mathbf{y}_{ci} + \mathbf{a}_{2i}\mathbf{h}_{ui} + \mathbf{a}_{3i}\mathbf{f}_{zzi} + \mathbf{a}_{4i}\mathbf{f}_{zpi}$$
(18)

In the literature [1] are given all values for the coefficients g, l and a Complete calculations, experimental results and producers catalogs give conclusion that in the rolling process with the steady rolling speeds "(without considerations of taking in (accelerating)» and staking out(slowing down)" the strip in (out) the rolling stand), the tension forces change smaller than 5% (lit [1]). Variations of the strip thickness which enters in the Cold Rolling Mill are very small because Sartid Hot Mill has electrohydraulic system for automatic gage control, too. Coefficients  $a_{2i}$ ,  $a_{3i}$  and  $a_{4i}$  are much smaller than coefficient a1 (reference [1]) and according to these conclusions we can write equation (19):

$$\mathbf{h}_{i} = \mathbf{a}_{1i} \mathbf{y}_{ci} \,. \tag{19}$$

### VIII. LINEAR MATHEMATICAL MODEL, BLOCK DIAGRAM AND STATE-SPACE REPRESENTATION OF THE SYSTEM

Linerisation of equations (3), (4), (5), (7), (10), (11) and equation (19) give linear mathematical model for a rolling stand:

Regulator: 
$$\mathbf{q}_{sr} = \mathbf{K}_{q}\mathbf{x}_{k} + \mathbf{K}_{c}\mathbf{p}_{c}, \ \mathbf{q}_{c} = \mathbf{A}_{c}\mathbf{y}_{c} + \frac{\mathbf{V}}{\mathbf{B}}\mathbf{p}_{c}, \ \mathbf{p}_{c}\mathbf{A}_{c} = \mathbf{m}_{c}\mathbf{y}_{c} + \mathbf{E}_{sr}\mathbf{y}_{c},$$
  
 $\mathbf{i} = \mathbf{x}_{k} + \mathbf{T}_{1}\mathbf{x}_{k}, (20)$ 

where: 
$$\mathbf{i} = \mathbf{K}_{A}(\mathbf{u}_{z} - \mathbf{u}_{MP}), \mathbf{T}_{u}\mathbf{u}_{MP} + \mathbf{u}_{mp} = \mathbf{K}_{pc}\mathbf{y}_{c}, \mathbf{u}_{z} = \mathbf{c}_{1}\mathbf{h}_{iz}$$
, object;  $\mathbf{h}_{i} = \mathbf{a}_{1}\mathbf{y}_{c}$ .

We can draw block diagram of the system for the automatic gage control of one rolling stand (figure 8) using system of equations (20):

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Define state variables:

$$\mathbf{x}_{1} = \mathbf{u}_{MP; \mathbf{x}_{2}} = \mathbf{y}_{c; \mathbf{x}_{3}} = \mathbf{y}_{c; \mathbf{x}_{4}} = \mathbf{x}_{K; \mathbf{x}_{5}} = \mathbf{p}_{c}$$
 (21)

Input and output are:

 $x_{u} = h_{iz}, x_{i} = h_{i}.(22)$ 

Notice that all state variables are easily measurable quantities (voltage from the position gage, piston rod velocity, piston rod position, servovalve spool position and the pressure in the cylinder). Output value is the change of the strip thickness and input value is demand change of the strip thickness. Then, from the definition of the state variables (21), equations (20) and figure 9, we obtain equations (23) and (24):

$$\dot{\mathbf{x}}_{1} = \frac{1}{T_{u}}\mathbf{x}_{1} + \frac{K_{pc}}{T_{u}}\mathbf{a}_{1}\mathbf{x}_{3}, \ \dot{\mathbf{x}}_{2} = -\frac{E_{sT}}{m_{c}}\mathbf{x}_{3} + \frac{A_{c}}{m_{c}}\mathbf{x}_{5}, \ \dot{\mathbf{x}}_{3} = \mathbf{x}_{2}, (23)$$

$$\dot{\mathbf{x}}_{4} = -\frac{\mathbf{K}_{A}}{\mathbf{T}_{1}}\mathbf{x}_{1} - \frac{1}{\mathbf{T}_{1}}\mathbf{x}_{4} - \frac{\mathbf{C}_{1}\mathbf{K}_{A}}{\mathbf{T}_{1}}\mathbf{x}_{u}, \\ \dot{\mathbf{x}}_{5} = -\frac{\mathbf{B}\mathbf{A}_{c}}{\mathbf{V}_{c}}\mathbf{x}_{2} - \frac{\mathbf{B}}{\mathbf{V}_{c}}\mathbf{K}_{q}\mathbf{x}_{4} + \frac{\mathbf{K}_{c}\mathbf{B}}{\mathbf{V}_{c}}\mathbf{x}_{5},$$
(23-1)

$$\mathbf{X}_{1} = \mathbf{a}\mathbf{X}_{3} \,. \tag{24}$$

### IX. SIMULATION OF THE SYSTEM WORK BY COMPUTER AND EXPERIMENTAL MEASUREMENTS IN REAL SYSTEM

According to system of equations (22) we obtain step response by computer (for the calculation of the all necessary coefficients we use dates from lit ([1,3]). For the same demand strip thickness change of  $0,5-10^{-3}$  mm was done series of experimental testing and result of that is shown at the figure 9, too. Comparison of this curves gives conclusion that nature of this curves are the same. Small difference between these curves is induced by impossibility of exactly determination and exactly testing the system characteristics.

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 $\frac{\Delta Y_{c}}{a} \begin{bmatrix} g^{2} \pi \end{bmatrix}$ 

Figure 9. Step responses obtained by simulation and experimental measurements in the plant

### X. CONCLUSION

Comparison of theoretical and experimental curves gives conclusion that all introduced assumptions are good. Analysis of the all system characteristics gives conclusion that system has good working. Electrohydraulic servosystem for the AGC has better characteristics than electromechanic system (five times greater speed of rolling, greater speed of positioning ,smaller dead–zone, smaller time of roll gap adjusting start, smaller time of maximum speed reaching,greater unloading speed...).

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